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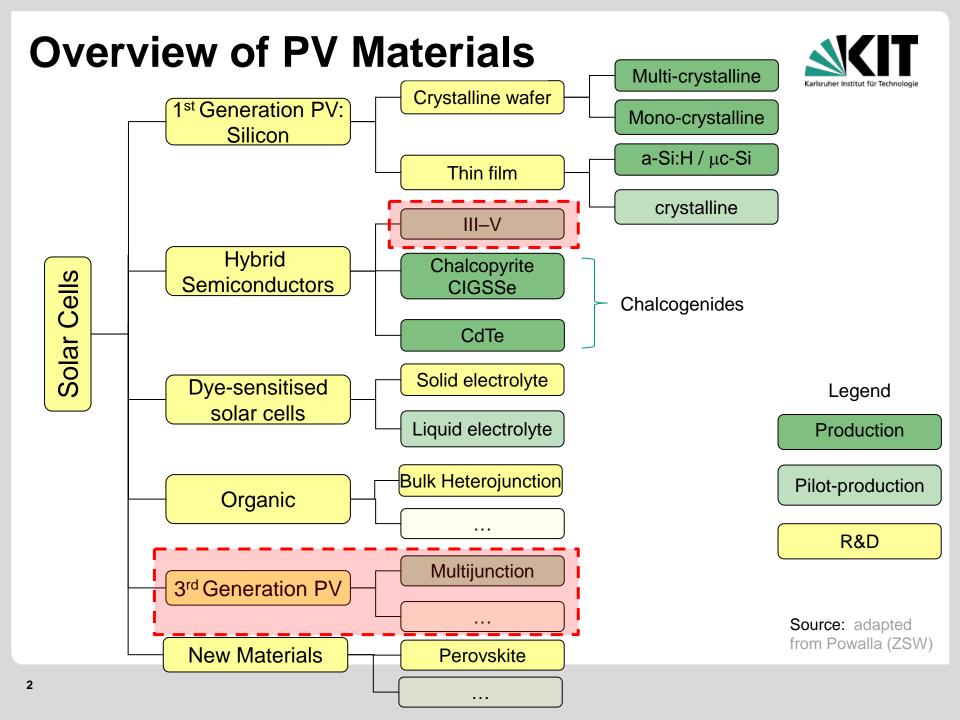
#### Lecture 12+13: Third Generation Photovoltaics

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KIT Focus Optics & Photonics

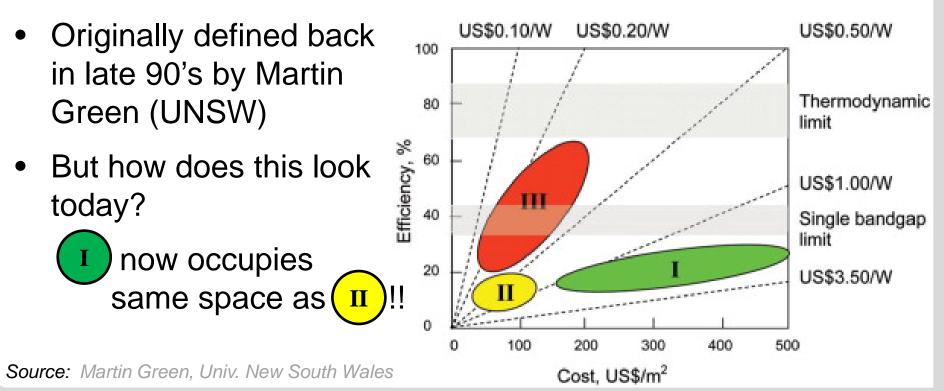


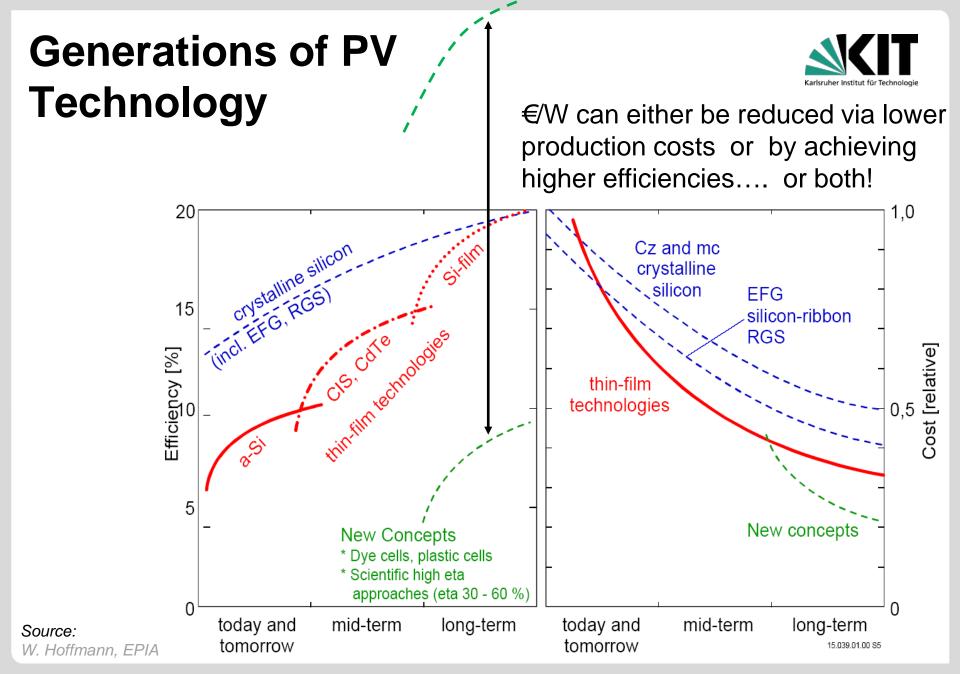


## **Generations of PV Technology**



- 1<sup>st</sup> gen: wafer-based silicon
- 2<sup>nd</sup> gen: single junction thin films
- 3<sup>rd</sup> gen: strategies to overcome single-junction limits, e.g. tandem (multijunction) solar cells





#### **Generations of PV Technology**



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 $\Rightarrow$  so what are the fundamental upper limits on solar energy conversion efficiency?



 Going back to thermodynamics: 1<sup>st</sup> and 2<sup>nd</sup> laws of thermodynamics as phrased by Rudolf Clausius in 1865:

"The total energy of the universe is constant. The total entropy of the universe strives to reach a maximum"

- Useful description of energy is: "The capacity for doing work. The various forms of energy ... include heat, chemical, nuclear and radiant energy. Interconversion between these forms of energy can occur only in the presence of matter. Energy can only exist in the absence of matter in the form of radiant energy".
- Matter itself is: "A specialised form of energy which has the attributes of mass and extension in space and time" (Lurarov and Chapman 1971).

Source: Martin Green, "Third Generation Photovoltaics: Advanced Solar Energy Conversion", Springer 2003



- Entropy: less intuitive concept, but is physically associated with disorder ⇒ less disorder ⇒ smaller entropy
- Clausius: entropy expressed as heat divided by temperature ⇒ transfer of a small amount of heat causes a larger change in entropy in a cold body than in a hot body
- In solar, normally have steady-state conditions and equilibrium between energy fluxes, rather than incremental transfers. Associated with an energy transfer as heat at rate  $\dot{E}$  to or from a body at temperature  $\ddot{T}$ , is an entropy flux  $\dot{E}/\dot{T}$ , if the transfer occurs in the presence of an infinitesimally small temperature differential.

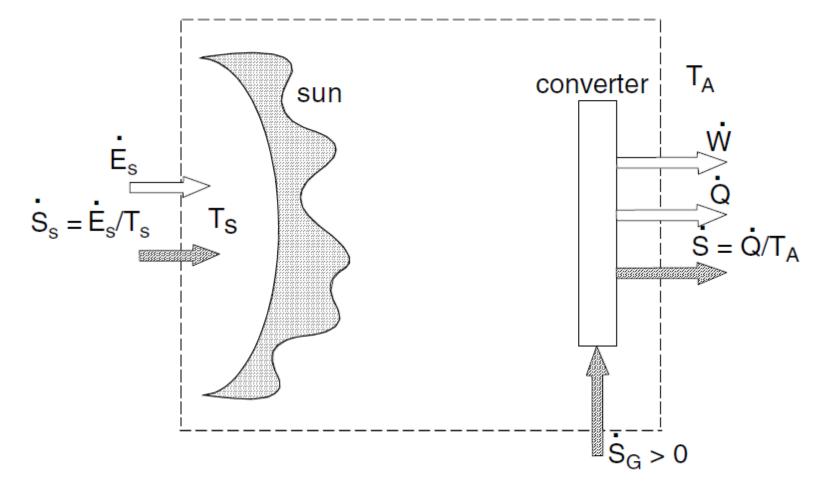
Source: Martin Green, "Third Generation Photovoltaics: Advanced Solar Energy Conversion", Springer 2003



- The most general efficiency limit for PV is the Carnot limit
- Inputs:  $\dot{E}_{s}$  = heat energy flux from sun's interior to fuel its radiative emission
  - $S_{s}$  = corresponding entropy flux, given by  $\dot{E}_{s}$  /  $T_{s}$
  - where  $T_S$  = temperature of sun's photosphere (6000K)
  - and  $\dot{S}_{G}$  = entropy generation flux associated with energy conversion (positive for any practical process)
- Outputs:  $\dot{W}$  = energy flux in the form of useful work with zero associated entropy flux
  - $\dot{Q}$  = heat flux rejected to the ambient, with associated entropy flux  $\dot{Q} / T_A$

where  $T_A$  = ambient temperature, 300K



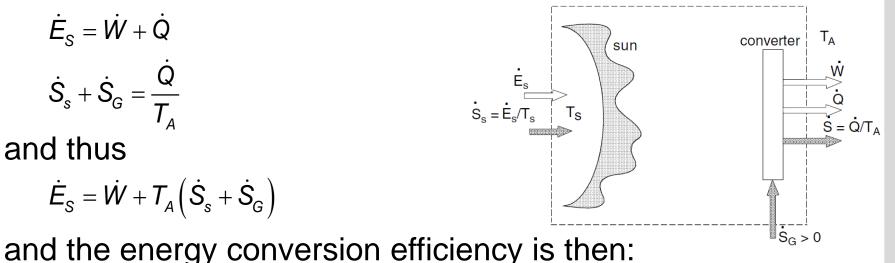


#### Fig. 3.1: System considered for calculating Carnot efficiency.

Source: Martin Green, "Third Generation Photovoltaics: Advanced Solar Energy Conversion", Springer 2003



 Can now express 1<sup>st</sup> and 2<sup>nd</sup> laws of thermodynamics as energy and entropy flux balance, respectively:



$$\eta = \frac{\dot{W}}{\dot{E}_{s}} = \left(1 - \frac{T_{A}}{T_{s}}\right) - \frac{T_{A}\dot{S}_{G}}{\dot{E}_{s}}$$

η has its maximum value of 95% when S<sub>G</sub> = 0,
 ⇒ Carnot efficiency for conversion of heat energy supplied to the sun's photosphere to terrestrial energy

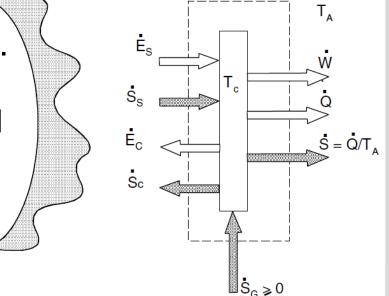


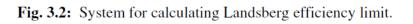
- Interesting point: no information is required about converter itself ⇒ natural question then is to whether there is any converter that could, at least in principle, achieve this limiting Carnot efficiency?
- Main requirement is no entropy generation during the transmission, absorption or conversion of the sunlight
- Planck showed that energy transfer between two blackbodies involves unavoidable entropy production, unless both are at same T ⇒ means finite entropy production in an absorber <u>unless absorber emits light of the same intensity</u> <u>as the sun at each wavelength</u>! But then there would be no net energy transfer! So, to achieve Carnot limit, only infinitesimally small amounts of work could be produced, with nearly all of the sun's energy being recycled



- The Landsberg  $\eta$  limit considers a more restricted system
- Inputs are <u>radiant energy</u> and associated entropy fluxes from the sun plus the unavoidable entropy generation during the absorption and conversion processes
- Outputs are again work and heat fluxes, plus associated entropy flux. Additional outputs are the <u>energy</u> <u>re-radiated</u> by the converter S<sub>c</sub> and associated entropy flux E<sub>c</sub>

$$\eta_{L} = 1 - \frac{4}{3} \frac{T_{A}}{T_{S}} + \frac{1}{3} \frac{T_{A}^{4}}{T_{S}^{4}} = 93.3\%$$
  
for  $T_{A} = 300K$ 





Source: Martin Green, "Third Generation Photovoltaics: Advanced Solar Energy Conversion", Springer 2003



 Black body η limit extends upon Landsberg analysis for reciprocal black-body absorbers ⇒ takes into account unavoidable entropy production during absorption and emission of light by the black-body S'<sub>G</sub>

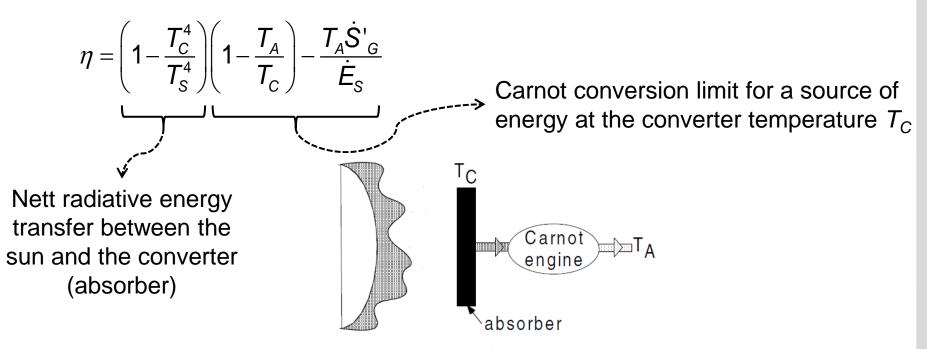
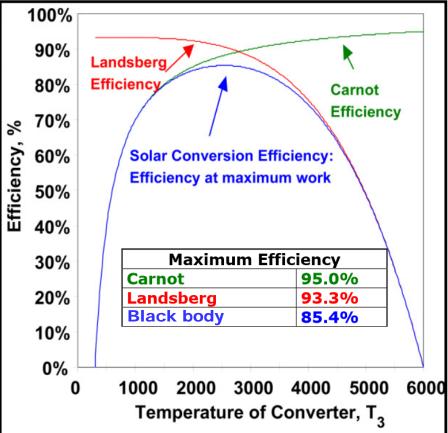


Fig. 3.3: Ideal solar thermal converter with sunlight absorbed by an absorber at temperature  $T_C$ , with heat extracted from this absorber converted to electricity by a Carnot converter.

Source: Martin Green, "Third Generation Photovoltaics: Advanced Solar Energy Conversion", Springer 2003



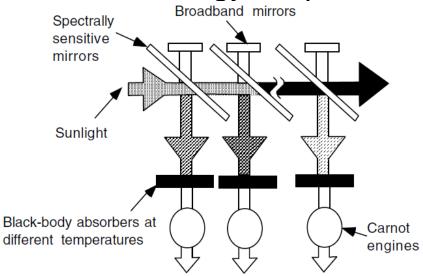
• For  $T_A / T_S = 0.05$  (300 K / 6000 K), the solution gives  $T_C / T_S$  equal to 0.424 or  $T_C = 2544$  K, corresponding to a maximum efficiency of 85.4%



Source: adapted from Christiana Honsberg, http://www.energy.udel.edu/pdf/Honsberg\_UDEI\_Symposium.pdf



 Emission from a black-body at each photon energy is determined solely by *T*, but higher efficiency is possible if emission of light at each energy is optimised separately

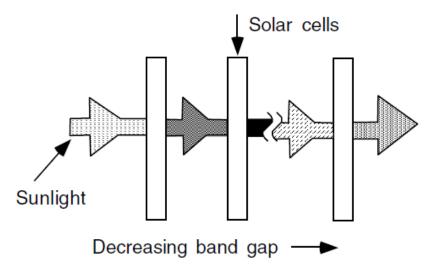


**Fig. 3.4:** Multicolour converter implemented using black-bodies and mirrors, both spectrally sensitive and broadband. The mirror arrangement shown ensures, in principle, that each black-body absorber both absorbs light over a narrow range of wavelengths, determined by the spectrally sensitive mirrors, and also has a nett emission over the same wavelength range.

#### $\Rightarrow \eta_{bb} = 86.8\%, \text{ so PV has a slight advantage over solar}$ thermal approaches Source: Martin Green, "Third Generation Photovoltaics: Advanced Solar Energy Conversion", Springer 2003



• Using tandem cell stacks, a conceptually equivalent geometry can be implemented much more elegantly



**Fig. 3.6:** Tandem cell stack giving the same limiting efficiency as the more complex system of Fig. 3.4.

 You have seen some practical implementations of this approach before (e.g. a-Si:H and OPV multi-junctions)



- Shockley-Queisser (SQ) efficiency limit for single *p-n* junction
- Starting point: an efficient solar cell needs to be an efficient absorber of solar photons and hence have properties related to a black-body, at least for  $E > E_g$ 
  - Attributed all this radiation for  $E > E_g$  to band-to-band recombination
  - Calculated the net rate of recombination in the cell taking into account photon recycling effects
  - Considered such a cell in thermal equilibrium (no external light on it and no voltage applied to it)
  - $\Rightarrow$  would have to be emitting Planckian black-body radiation at these energies



 SQ could now calculate the net recombination rate at any voltage ⇒ leads to ideal solar cell equation with unity ideality factor (N = 1), area A and I<sub>0</sub> given by:

$$I_o = qA\dot{N}(E_G,\infty) \approx qA(\frac{2\pi kT}{h^3 c^2}) \left[ E_G^2 + 2(kT)E_G + 2(kT)^2 \right] e^{-E_G/kT}$$

- Assumptions in this "detailed balance" approach:
  - i) The mobility  $\mu$  is infinite  $\Rightarrow$  collection of carriers no matter where they are generated
  - ii) Complete absorption of all photons above the band gap
  - iii) That  $E_G >> kT$



• If sun is modelled as a black-body at temperature  $T_s \Rightarrow I - V$  curve can be expressed as:

 $I = qAf_s \dot{N}(E_G, \infty, T_s) - qA f_c \dot{N}(E_G, \infty, T_c) (e^{qV/kT} - 1)$ 

where

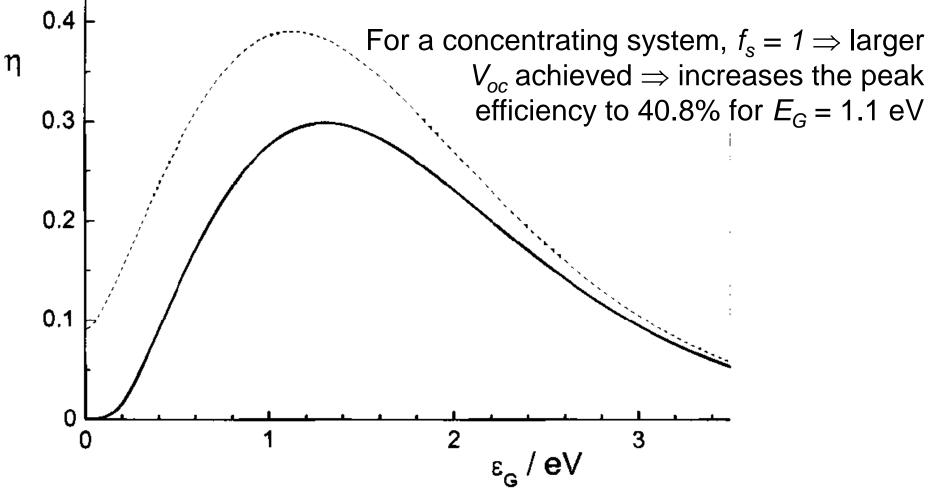
 $f_s = 1$  for a system under maximum solar concentration (46200, calculated from  $C_{ideal} \leq n^2 / \sin^2 \delta$  with angular diameter of the sun  $\delta = 32$  arc minutes)

 $f_c = 1$  for a solar cell with maximum angular selectivity

• For the non-concentrating system analysed by SQ, the solar intercept fraction  $f_s = 2.1646 \times 10^{-5}$  and  $f_c = 1$ 

⇒ peak efficiency of 
$$\eta_{SQ}$$
 = 31.0% for  $E_G$  = 1.3 eV for  $T_S$  = 6000 K and  $T_C$  = 300 K





**Figure 7.2:** Efficiency of solar cells with radiative recombination only as a function of their energy gap for the *AM*0 spectrum, non-concentrated (solid line) and for full concentration (dashed line).

Source: Peter Würfel, "Physics of Solar Cells", Wiley 2005

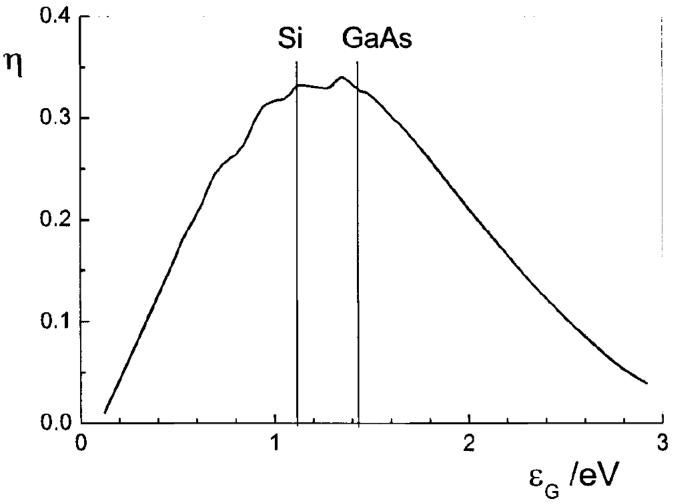
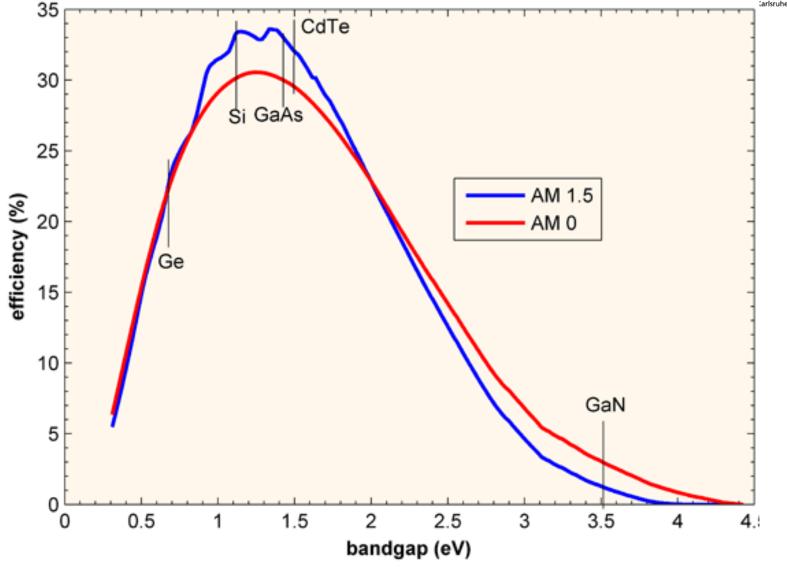


Figure 7.3: Efficiency of solar cells with radiative recombination only as a function of the energy gap for the AM1.5 spectrum.

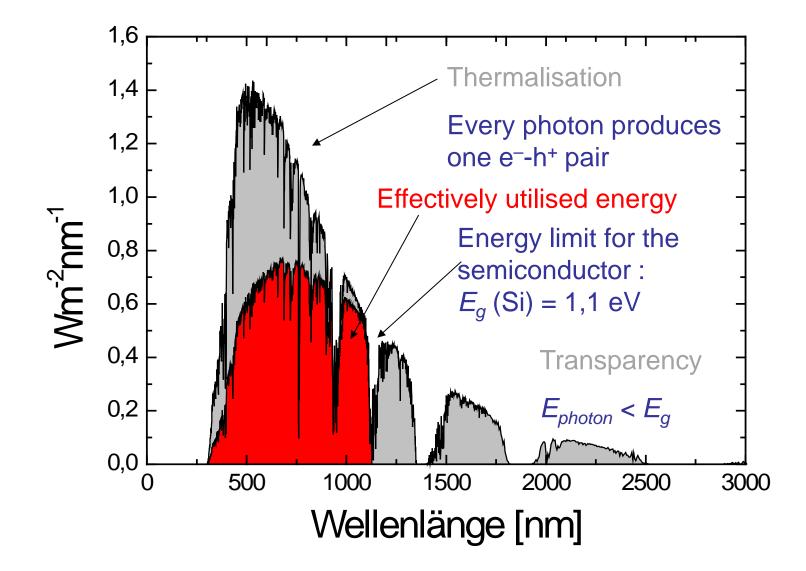
Source: Peter Würfel, "Physics of Solar Cells", Wiley 2005





#### Die Absorption der "Sonnenphotonen"





**Table 5.1:** Limiting efficiencies and optimal bandgaps for a range of tandem cell designs (Marti and Araujo 1996; Brown 2002).

No. of Cells	Description	Optimal Bandgaps (eV)						Effic %
		E1	E2	E3	E4	E5	E6	
1	Diffuse	1.31						31.0
	Direct	1.11						40.8
2	Diffuse, series connected	0.97	1.70					42.5
	Diffuse, unconstrained	0.98	1.87					42.9
	Direct, series connected	0.77	1.55					55.5
	Direct, unconstrained	0.77	1.70					55.9
3	Diffuse, series connected	0.82	1.30	1.95				48.6
	Diffuse, unconstrained	0.82	1.44	2.26				49.3
	Direct, series connected	0.61	1.15	1.82				63.2
	Direct, unconstrained	0.62	1.26	2.10				63.8
4	Diffuse, series connected	0.72	1.10	1.53	2.14			52.5
	Diffuse, unconstrained	0.72	1.21	1.77	2.55			53.3
	Direct, series connected	0.51	0.94	1.39	2.02			67.9
	Direct, unconstrained	0.52	1.03	1.61	2.41			68.8
5	Diffuse, series connected	0.66	0.97	1.30	1.70	2.29		55.1
	Diffuse, unconstrained	0.66	1.07	1.50	2.03	2.79		56.0
	Direct, series connected	0.44	0.81	1.16	1.58	2.18		71.1
	Direct, unconstrained	0.45	0.88	1.34	1.88	2.66		72.0
6	Diffuse, series connected	0.61	0.89	1.16	1.46	1.84	2.41	57.0
	Diffuse, unconstrained	0.61	0.96	1.33	1.74	2.26	3.00	58.0
	Direct, series connected	0.38	0.71	1.01	1.33	1.72	2.31	73.4
	Direct, unconstrained	0.40	0.78	1.17	1.60	2.12	2.87	74.4
∞	Diffuse (unconstrained, series							68.2
	connected, 2-terminal) Direct (unconstrained, series connected, 2-terminal)							86.8

# Tandem cells can achieve $\eta$ up to 86.8% for an infinite number of cells!

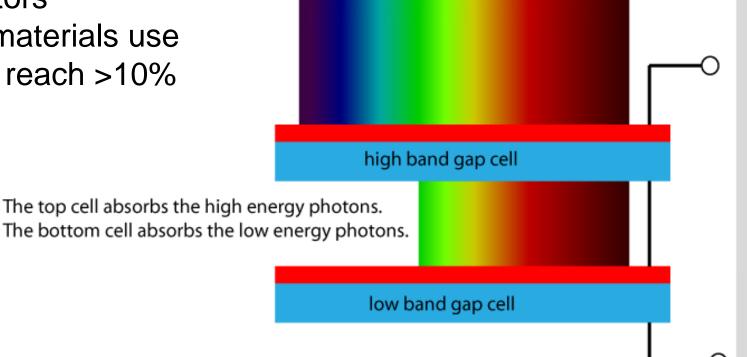
Source: Martin Green, "Third Generation Photovoltaics: Advanced Solar Energy Conversion", Springer 2003





- Multiple materials used for tandems  $\Rightarrow$  primarily III-V and alloys from the a-Si-C-Ge system
- III-V materials used to achieve ultra-high efficiencies, often in concentrators
- Low cost materials use tandem to reach >10%

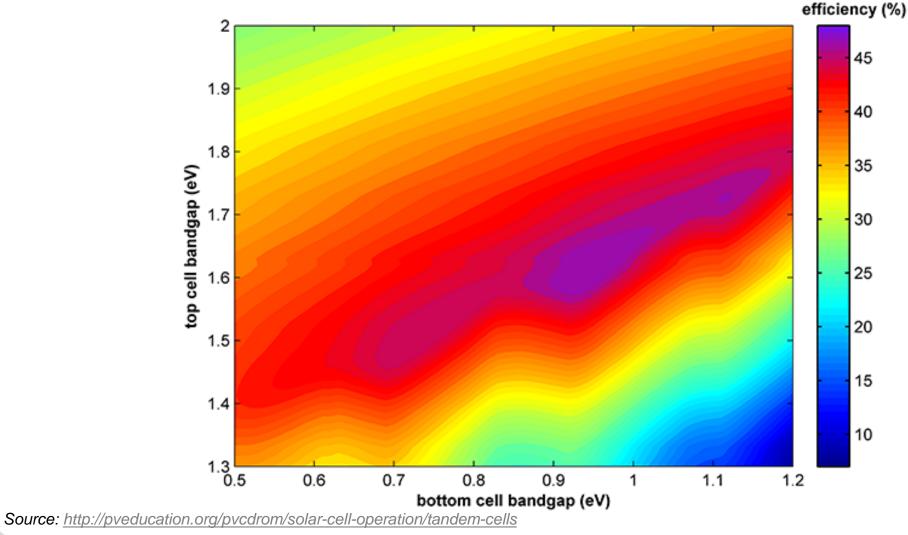
incoming full spectrum



Source: http://pveducation.org/pvcdrom/solar-cell-operation/tandem-cells

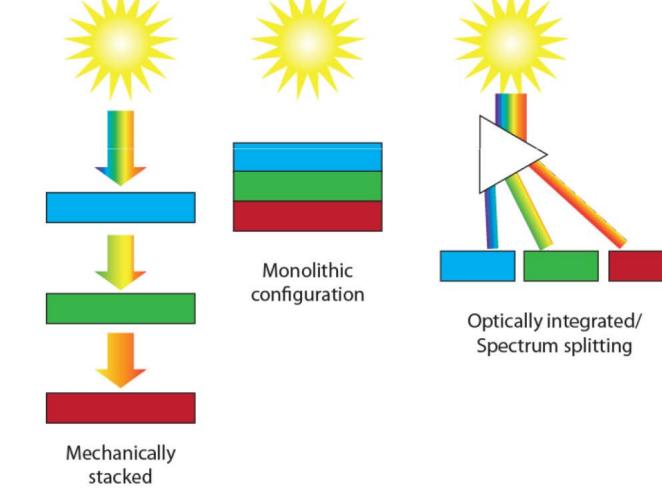


• Ideal bandgaps for double junction

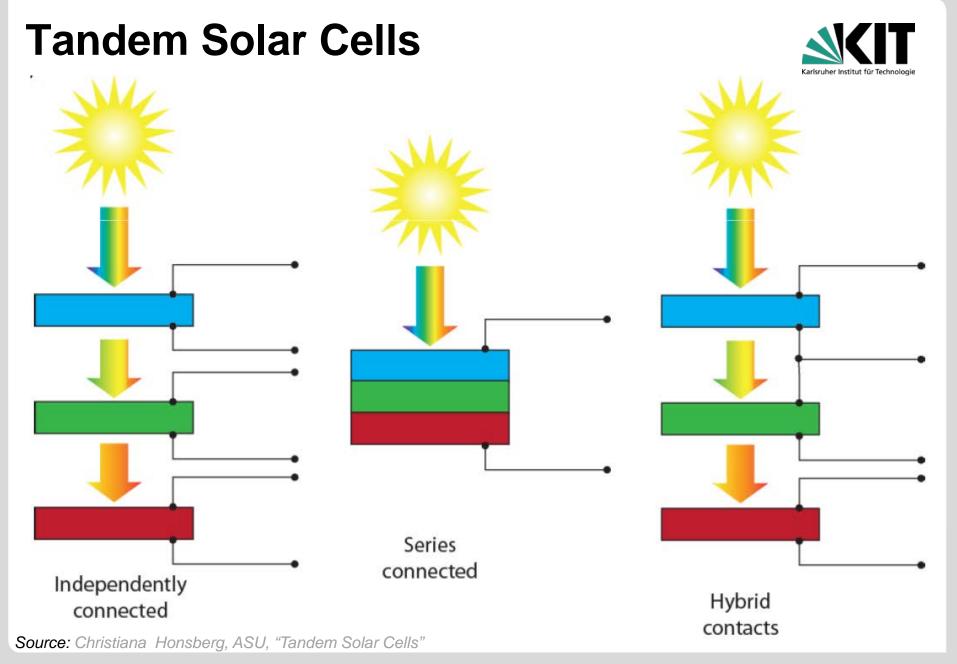




Many configurations for optically integrated or spectrum split devices



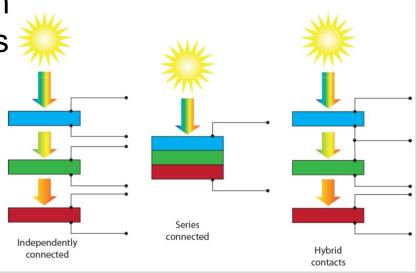
Source: Christiana Honsberg, ASU, "Tandem Solar Cells"





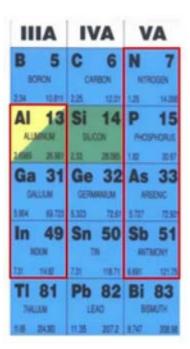
- Electrical interconnection impacts the theoretical efficiency (small effect), optimum materials, and device design
- Approaches other than series connected introduce additional cost and complexity into power electronics (and also typically solar cell design), so monolithic, series connected devices are most commonly implemented
- Series connected requires current matching and places substantial constraints on tandem efficiency by limiting the materials
   that can be used
- Other approaches not used in practice

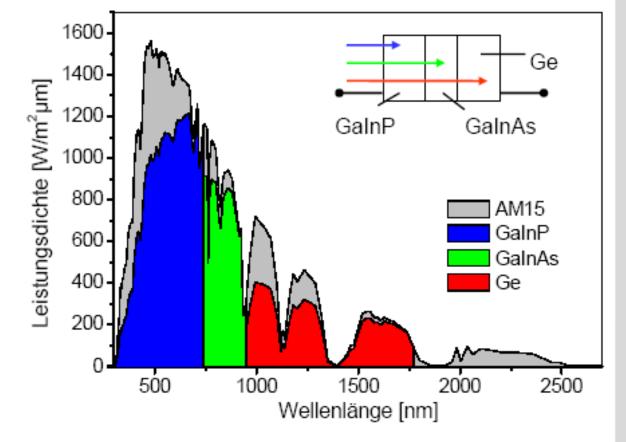
Source: Christiana Honsberg, ASU, "Tandem Solar Cells"





 Minimise lattice thermalisation and transparency losses – example of GaInP / GaInAs / Ge triple-junction solar cell





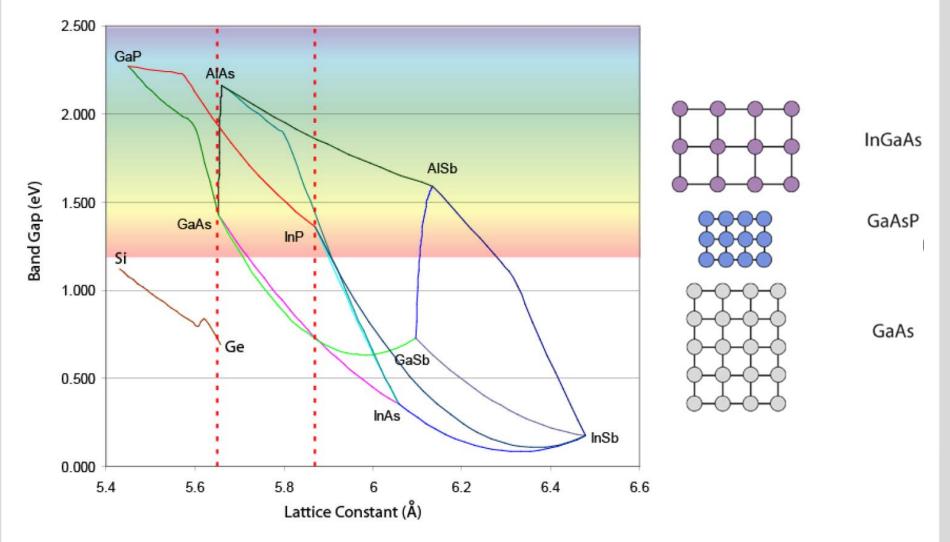


- Realising high efficiency requires nearly ideal solar cells of desired bandgaps  $\Rightarrow$  each has high minority carrier lifetime
- Major design constraint are:
  - Series connection ⇒ lowest maximum power current limits the overall power
  - Closely lattice matched solar cell materials ⇒ high material quality which in turn means materials must be closely lattice matched
  - Overall, tandems highly dependent on material availability and quality.
- Design constraints impact number of solar cells in stack, theoretical efficiency of tandem, and (through material quality) fraction of theoretical efficiency achieved



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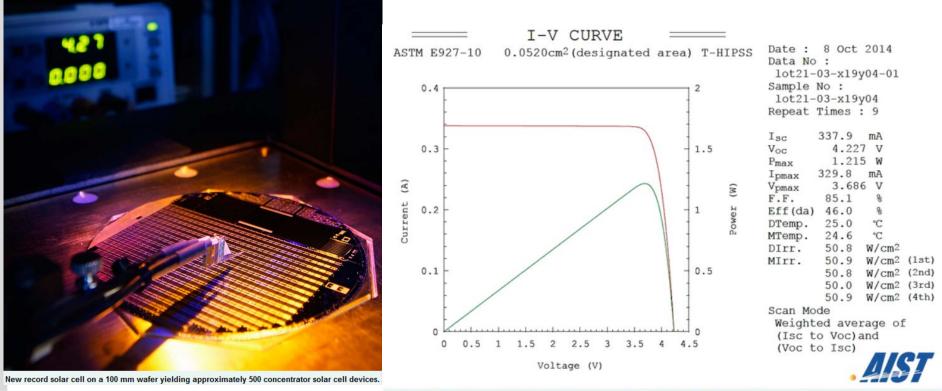




Source: Christiana Honsberg, ASU, "Tandem Solar Cells"



 New world record of 46% efficient solar cell (4 junctions) on 1<sup>st</sup> Dec – by Soitec and CEA-Leti, France, together with the Fraunhofer Institute for Solar Energy Systems

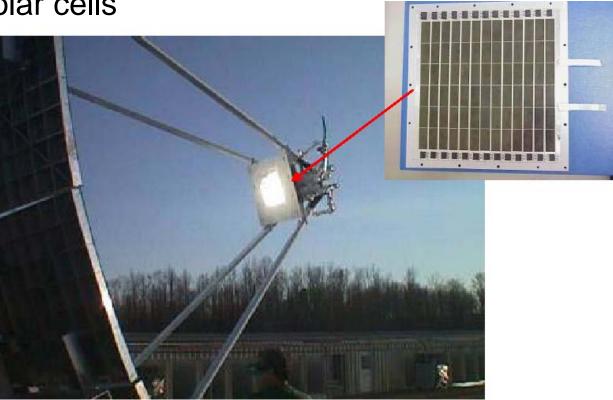


IV characteristics of the new 4-junction solar cell with an efficiency of 46% at 50.8 W/cm2 which corresponds to a concentration ration of 508 times the solar AM1.5d (ASTM E927-10) spectrum.

Source: http://www.ise.fraunhofer.de/en/press-and-media/press-releases/press-releases-2014/new-world-record-for-solar-cell-efficiency-at-46-percent



- Such high efficiency solar cells are used in high concentration, two-axis tracking systems
- High concentration means small area (and lower cost) needed for solar cells
- Trade-off between the costs of i) solar cell and ii) balance of the systems (BoS) components



Source: Christiana Honsberg, ASU, "Tandem Solar Cells"

#### **Hot Carrier Solar Cells**



 Idea: extract excess energy from high-energy charge carriers energy they thermalise back down to band edges

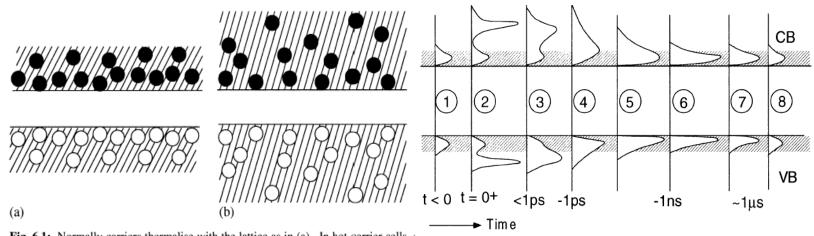


Fig. 6.1: Normally carriers thermalise with the lattice as in (a). In hot carrier cells, ( energy is stored in a hot carrier distribution, as shown in (b).

**Fig. 6.2:** Time evolution of electron and hole distributions in a semiconductor subject to a short, high intensity, monochromatic pulse of light from a laser: (1) Thermal equilibrium before pulse; (2) "coherent" stage straight after pulse; (3) carrier scattering; (4) thermalisation of "hot carriers"; (5) carrier cooling; (6) lattice thermalised carriers; (7) recombination of carriers; (8) return to thermal equilibrium.

## Hot carriers may be able to travel 10nm before they thermalise

Source: Martin Green, "Third Generation Photovoltaics: Advanced Solar Energy Conversion", Springer 2003

#### **Hot Carrier Solar Cells**



- How to achieve this??
- One idea (Würfel): use a wide bandgap semiconductor with narrow conduction and valence bands

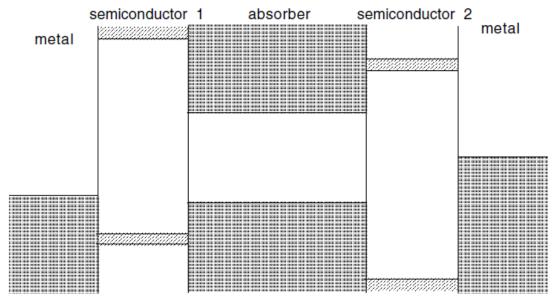
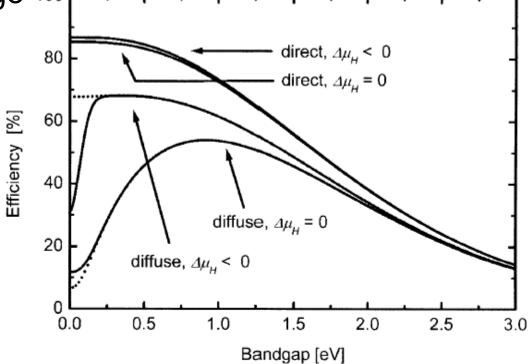


Fig. 6.3: Selective energy contacts to hot carrier cell based on wide bandgap semiconductors with narrow valence (left) and conduction (right) bands.

Maybe also possible using quantum dots

## **Hot Carrier Solar Cells**





**Fig. 6.7:** Limiting efficiency of a hot carrier cell for direct and diffuse sunlight. The curves labelled  $\Delta \mu_H < 0$  show the unconstrained case while the curves labelled  $\Delta \mu_H = 0$  shows the case where there are high levels of interaction between hot electrons and holes.



#### **Impact Ionisation**



 Idea: to generate more than one e<sup>-</sup>-h<sup>+</sup> pair per high energy photon ⇒ quantum efficiency can now be >100%!

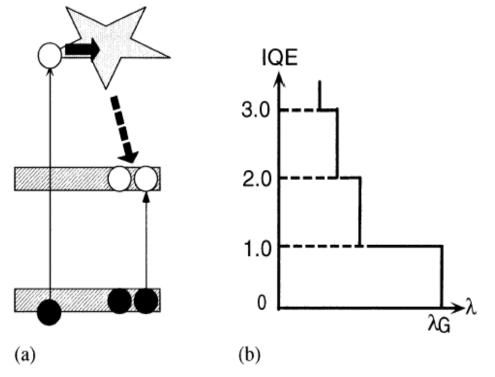


Fig. 7.1: (a) Schematic of the impact ionisation process whereby one energetic photon creates multiple electron-hole pairs; (b) Energetically feasible internal quantum efficiency, where  $\lambda_G$  is the wavelength corresponding to the threshold energy for electron-hole pair creation.

# **Impact Ionisation**



- If impact ionization occurs, we must also consider the reverse process Auger recombination
- Main point: all of the absorbed energy remains in the electronic system and the thermal losses are very small

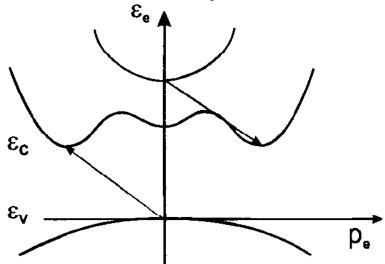


Figure 8.8: Transition of an electron from a higher band to the minimum of the conduction band by impact ionization in an indirect semiconductor, resulting in the additional generation of an electron and a hole at the band edges.

Source: Peter Würfel, "Physics of Solar Cells", Wiley 2005

## **Impact Ionisation**



 Again, very high efficiencies theoretically possible, even for unconcentrated sunlight (lower curve)

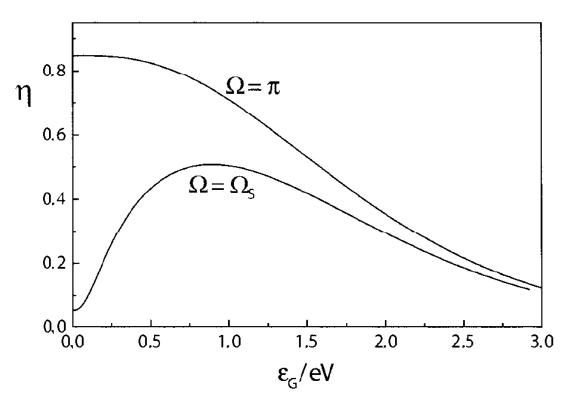


Figure 8.10: Efficiency for a hot carrier cell with impact ionization for non-concentrated incident solar radiation with  $\Omega = \Omega_S$  and for maximum concentration with  $\Omega = \pi$ .

Source: Peter Würfel, "Physics of Solar Cells", Wiley 2005



Way of addressing sub-bandgap transparency losses
 ⇒ impurity photovoltaic (IPV) device

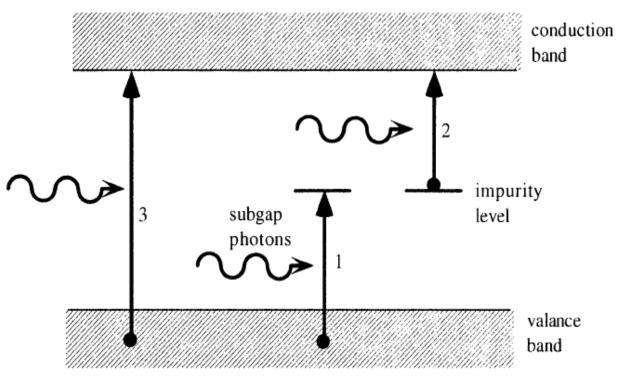


Fig. 8.1: Impurity photovoltaic effect where electron-hole pairs are generated by subbandgap photons (Keevers and Green 1994).



Way of addressing sub-bandgap transparency losses
 ⇒ intermediate band solar cell

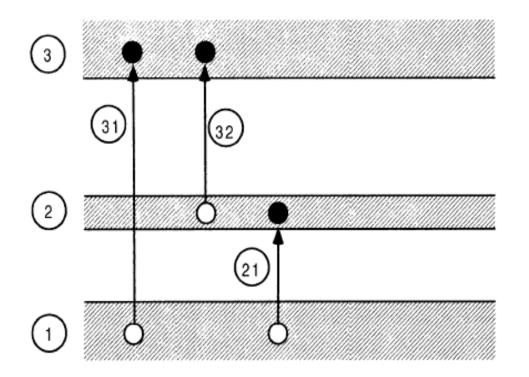
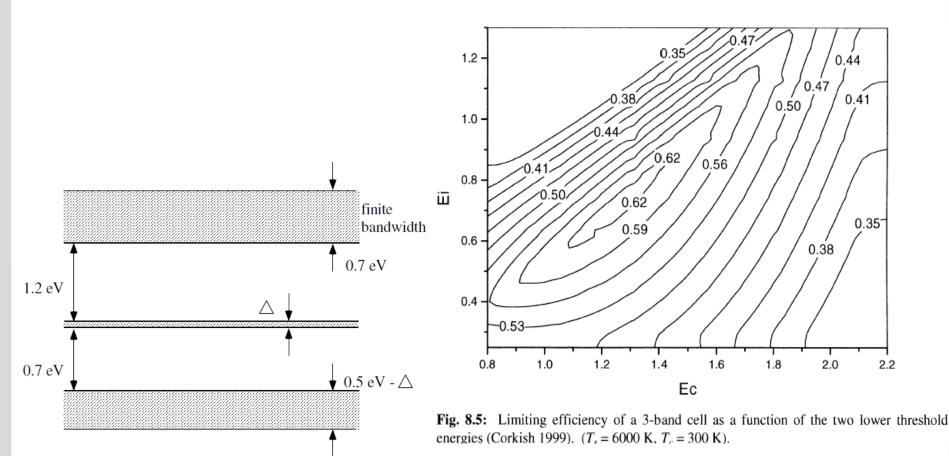


Fig. 8.3: 3-band solar cell. The lower- and upper-most bands are valence and conduction bands, while the intermediate band is considered to be an impurity band.



• High efficiencies again possible with three bands....



**Fig. 8.6:** Optimally designed 3-band cell with photon selectivity ensured by finite bandwidth for each of the 3 bands involved.



Way of addressing sub-bandgap transparency losses
 ⇒ impurity photovoltaic (IPV) device

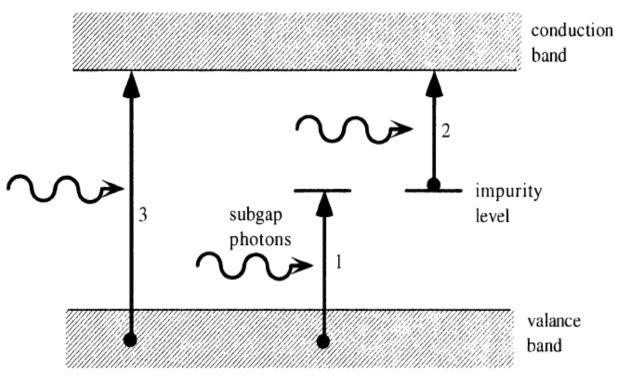


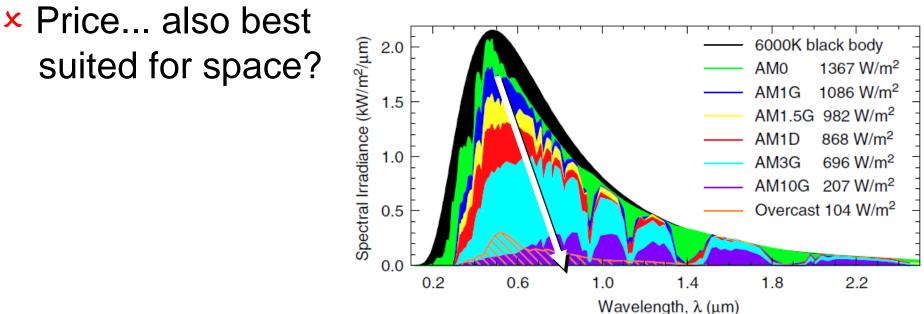
Fig. 8.1: Impurity photovoltaic effect where electron-hole pairs are generated by subbandgap photons (Keevers and Green 1994).

## **Briefly back to Tandems**



#### <u>Disadvantages</u>

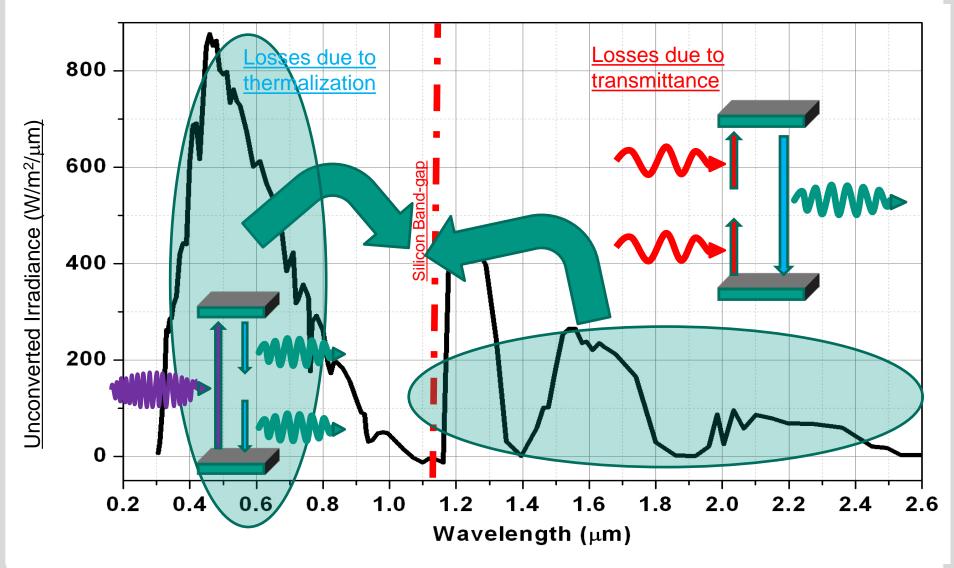
- × Solar cells connected in series  $\Rightarrow$  current matching problem with varying AM
- x Best suited for non-varying sunlight  $\Rightarrow$  space



⇒ What can be achieved with spectral conversion?

#### **Spectral Conversion**



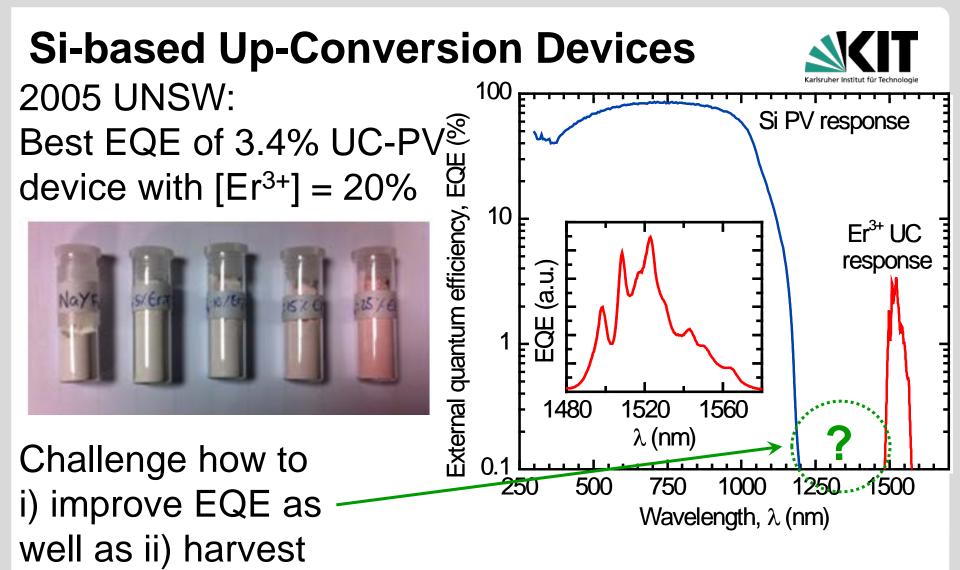


# **Up-Conversion**



Up-conversion of 2 low-E photons to give 1 higher-E photon  $\Rightarrow$  overcomes sub-bandgap losses BUT additional recombination  $\lambda_{\text{exc}}$ paths not introduced  $\lambda_{exc} > \lambda_{em}$ **Up-conversion** 20  $-4S_{3/2}$ (- us) (15 ° 9/2 3 9/2 <sup>0</sup>도 10 11/2 2 ENERGY 13/2 5 540nm 980nm 810nm 660nm 550nm Bifacial Si solar cell (1) 2  $\eta = 15-20\%$ 0 15/2 UC: NaYF<sub>4</sub>:Er<sup>3+</sup> Er <sup>3+</sup> Er <sup>3+</sup> in polymer Rear reflector 48

[Shalav, Richards, et al., APL 86 (2005) 103505]



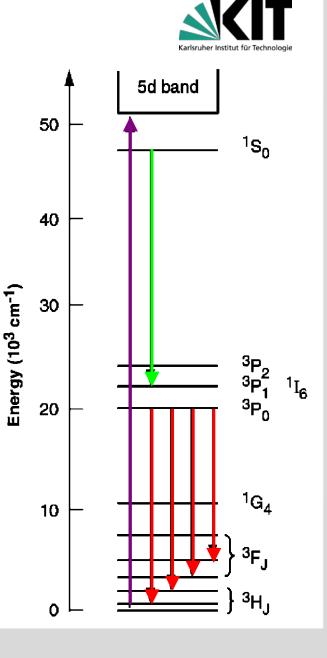
[Shalav, Richards, et al., Appl. Phys. Lett. 86 (2005) 103505 Richards, Shalav, IEEE Trans. Elec. Dev. 54 (2007) 2679 – 2684 Shalav, Richards, Green, Sol.En.Mat.Sol.Cell 91 (2007) 829–842 ]

light?

1200 – 1500nm

# **Down-Conversion**

- DC already used in other industries
- While fluorescent lamp phosphors based on Pr<sup>3+</sup> ion achieve quantum yields of 140%, several challenges remain for PV:
  - No deep UV light in solar spectrum!
  - Lanthanide ions are weak absorbers
     ⇒ current layers would be ~1cm thick

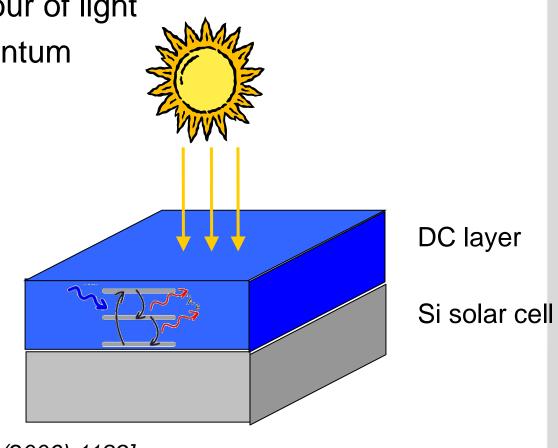


[adapted from Ronda, J. Alloys Comp. 225 (1995) 534]

#### **Down-Conversion**

- But for PV there are some advantages:
  - DC is linear process
  - Don't care about colour of light
- Can we realise 200% quantum efficiencies...??





[Richards, Sol.En.Mat.Sol.Cells 90 (2006) 1189]